## A Processing Ghost in a Tank Machine

## Mario Fifić



Air Force Research Laboratory, Cognitive Lunch Brown Bag, November, 2013

## A Processing Ghost in a Tank Máchine



Air Force Research Laboratory, November, 2013



Pred polazak na zadatak: avion F-84G, ev. broj 10602, sa

## Research Perspectives

Mario Fifić<br>Grand Valley State University, MI

- My research interests center on developing a process-tracing approach that allows for precise determination of the fundamental properties of the mental processes that underlie cognitive actions.


## Theoretical advances

# Logical-Rule Models of Classification Response Times: A Synthesis of Mental-Architecture, Random-Walk, and Decision-Bound Approaches 

## Mario Fific

Max Planck Institute for Human Development

Daniel R. Little and Robert M. Nosofsky Indiana University, Bloomington


# A magnifying glass on human cognition 

Information-Processing Alternatives to Holistic Perception: Identifying the Mechanisms of Secondary-Level Holism Within a Categorization Paradigm

Mario Fifić
Max Planck Institute for Human Development

James T. Townsend Indiana University Bloomington


## The applications



## 9

Assessment of Mental Architecture in Clinical/Cognitive Research

James T. Townsend and Mario Fifić
Indiana University
Richard W. J. Neufeld
University of Western Ontario

## A HANDBOOK OF PROCESS TRACING METHODS FOR DECISION RESEARCH

a Critical review and user's guide
Edited by
Michael Schulte-Mecklenbeck Anton Kühberger

Rob Ranyard

## Part III: Methods for Tracing Physiological, Neurological, and Other Concomitants of Cognitive Processes <br> 139

6 Analyzing Response Tìmes to Understand Decision Processes 141
Wolfgang Gaissmaier, Mario Fific, and Jörg Rieskamp

SOCIETY FOR JUDGMENT

## Motivation

- Understanding mind's cognitive mechanism
- Understanding the brain's neural mechanisms
- Assessment of individuals with application in Clinical, Personality, Developmental Psychology


## Stopping Rule Selection (SRS) Theory Applied to Deferred Decision Making



Mario Fifić
Grand Valley State University

## Marcus Buckmann

Max Planck Institute for Human Development, Center for Adaptive Behavior and Cognition, Berlin


## A Processing Ghost in a Tank Machine

## Mario Fifić

# Grand Valley State University Michigan 

Air Force Research Laboratory, November, 2013

## Working memory (WM) under consideration

- Processing order
- Capacity status
- Subdivision by modalities
- Dual or one system
- Status of mental representations \& resource allocation


## Resource allocation models of WM

- The discrete-slot model proposes that WM operates on the ALL-OR-NONE principle: holding only highresolution item representations stored in a limited number of memory slots.
- The slots+averaging model is variant of the discrete-slot model assuming that more than one slot could be allocated to a single item representation
- the variable-resources model WM operates on the ALL-GET-SOME principle: a pool of limited resources is dynamically allocated across a set of memorized items representations.



## Why status of mental representations?

- Resource allocation.
- If representations are ALL-OR-NONE, and the system's capacity is limited, then when there is information overload an operator must guess.
- Sophisticated guessing?
- Neural system's implications.


## Resource allocation in model of WM



## Evidence supporting Discrete Slots Model

- Zhang \& Luck 2008
- Cowan (2001) The magical number 4 in short-term memory
- Rouder, Morey, Cowan, Zwilling, Morey, \& Pratte (2008).
- Donkin, Nosofsky, Gold, \& Shiffrin, (in press 2013).






## Evidence supporting the Variable-resource model

- van den Berg, R., Shin, H., Chou, W.C., George, R., \& Ma, W.J. (2012)
- Bays \& Husain (2008)


C



## van den Berg, et al. (2012). Appendix..

ments $\mathbf{x}=\left(x_{1}, \ldots, x_{N}\right)$ and $\mathbf{y}=\left(y_{1}, \ldots, y_{N}\right)$, we use a Bayesianobserver model. The Bayesian observer computes a probability distribution over the location of the change, $p(L \mid \mathbf{x}, \mathbf{y})$, and then reports the location with the highest probability. The posterior distribution over $L$ is proportional to the joint distribution, $p(x, y$, $L$ ), which in tum is evaluated as an integral over the remaining variables, namely $\Delta, \theta$, and $\varphi$,

$$
\begin{aligned}
p(\mathbf{x}, \mathbf{y}, L) & =\iiint p(\mathbf{x}, \mathbf{y}, \boldsymbol{\theta}, \boldsymbol{\varphi}, \Delta, L) d \Delta d \boldsymbol{\theta} d \varphi \\
& =\iiint p(L) p(\Delta) p(\boldsymbol{\theta}) p(\boldsymbol{\varphi} \mid L, \boldsymbol{\theta}) p(\mathbf{x} \mid \boldsymbol{\theta}) p(\mathbf{y} \mid \boldsymbol{\varphi}) d \Delta d \boldsymbol{\theta} d \boldsymbol{\varphi}
\end{aligned}
$$

where in going from the first to the second line we have used the structure of the generative model in Fig. S1B. Substituting distributions and evaluating the integral over $\varphi$ gives

$$
\begin{equation*}
p(\mathbf{x}, \mathbf{y}, L)=\frac{1}{N}\left(\frac{1}{2 \pi}\right)^{N+1} \int \prod_{i=1}^{N}\left(\int p\left(x_{i} \mid \theta_{i}\right) p\left(y_{i} \mid \varphi_{i}=\theta_{i}+\Delta \delta_{L, i}\right)\right) d \Delta \tag{S16}
\end{equation*}
$$

where $\delta_{L i}=1$ when $L=i$ and 0 otherwise. Because we are interested only in the dependence on $L$, we can freely divide by the $L$-independent product $\prod_{i=1}^{N}\left(\int p\left(x_{i} \mid \theta_{i}\right) p\left(y_{i} \mid \varphi_{i}=\theta_{i}\right)\right)$, leaving only integrak pertaining to the $L$ th location:

$$
p(\mathbf{x}, \mathbf{y}, L) \propto \frac{\iint p\left(x_{L} \mid \theta_{L}\right) p\left(y_{i} \mid \varphi_{L}=\theta_{L}+\Delta\right) d \theta_{L} d \Delta}{\int p\left(x_{L} \mid \theta_{L}\right) p\left(y_{L} \mid \varphi_{L}=\theta_{L}\right)}
$$

that is among the encoded ones. In analogy to Eq. S16, this probability is

$$
\begin{align*}
& (L \text { encoded }) p(\mathbf{x}, \mathbf{y}, L)=\frac{1}{N}\left(\frac{1}{2 \pi}\right)^{K+1}  \tag{S19}\\
& \times \int \prod_{i=1}^{K}\left(\int p\left(x_{i} \mid \theta_{i}\right) p\left(y_{i} \mid \varphi_{i}=\theta_{i}+\Delta \delta_{L i, i}\right)\right) d \Delta
\end{align*}
$$

Now we evaluate the joint probability of $\mathbf{x}, \mathbf{y}$ and that the change occurred at a location $L$ that is not among the encoded ones. This probability is equal to
( $L$ not encoded) $p(\mathbf{x}, \mathbf{y}, L)=\iint p(\mathbf{x}, \mathbf{y}, \boldsymbol{\theta}, \boldsymbol{\varphi}, L) d \boldsymbol{\theta} d \boldsymbol{\varphi}$

$$
\begin{align*}
& =\iint p(L) p(\boldsymbol{\theta}) p(\boldsymbol{\varphi} \mid L, \boldsymbol{\theta}) p(\mathbf{x} \mid \boldsymbol{\theta}) p(\mathbf{y} \mid \boldsymbol{\varphi}) d \boldsymbol{\theta} d \boldsymbol{\varphi} \boldsymbol{\varphi} \\
& \quad=\frac{1}{N}\left(\frac{1}{2 \pi}\right)^{K} \prod_{i=1}^{K}\left(\int p\left(x_{i} \mid \theta_{i}\right) p\left(y_{i} \mid \varphi_{i}=\theta_{i}\right)\right) \tag{S20}
\end{align*}
$$

As one would expect, this probability does not depend on $L$. Because we are interested only in the location $L$ for which $p(\mathrm{x}, \mathrm{y}$, $L$ ) is largest (i.e., the argmax), we divide both Eqs. S19 and S20 by Eq. S20. Then, in analogy to Eq. S17, we have to take the argmax of

$$
\begin{cases}(L \text { encoded }) & \frac{1}{2 \pi} \frac{\iint p\left(x_{L} \mid \theta_{L}\right) p\left(y_{i} \mid \varphi_{L}=\theta_{L}+\Delta\right) d \theta_{L} d \Delta}{\int p\left(x_{L} \mid \theta_{L}\right) p\left(y_{L} \mid \varphi_{L}=\theta_{L}\right)}=\frac{1}{2 \pi \int p\left(x_{L} \mid \theta_{L}\right) p\left(y_{L} \mid \varphi_{L}=\theta_{L}\right)} \\ (L \text { not encoded }) & 1 .\end{cases}
$$

## Unresolved question(s)

 (what's under the all-or-none carpet)- (1) We argue that the above research advances have been downplaying the experimental approaches to directly manipulate the allocation of resources across item representations held by WM.
- Our study showed that, when instructed, subjects adaptively allocated a limited amount of resources and shared them across memorized item representations.

Unresolved question(s) (what's under the carpet)

- (2) The exact mechanism of resource allocation has not been specified.


## Specific Research Questions

DHow are the resources allocated in WM? (HalfHalf rule)

What is the status of mental representations in WM?

## How are the capacity resources

 allocated? Attentional gating function in STMEqual


Ascending



## How are the capacity resources distributed? <br> The Half-Half Optimal Rule

- The optimal solution for allocation of a limited amount of resources: one Half of resources should be allocated to memorized items and another Half to a target.

$$
\begin{aligned}
& \underset{\text { Target }}{\arg \max }\left[\sum_{\mathrm{i}}^{\mathrm{N}-1} \text { Target } \cdot \text { Item }_{i}\right] \\
& \sum_{\mathrm{i}}^{\mathrm{N}-1} \operatorname{Target} \cdot \text { Item }_{i}=\operatorname{Target} \sum_{\mathrm{i}}^{\mathrm{N}-1} \text { Item }_{i}=\operatorname{Target}(\text { TotalCapacity }- \text { Target })= \\
& \text { Target } \cdot \text { TotalCapacity - Target }{ }^{2} \\
& \frac{d}{d \text { Target }}\left[\text { Target } \cdot \text { TotalCapacity }- \text { Target }^{2}\right]=\text { TotalCapacity }-2 \cdot \text { Target } \\
& \text { TotalCapacity }-2 \cdot \text { Target }=0 \\
& \text { Target }=\frac{1}{2} \text { TotalCapacity }
\end{aligned}
$$

## The Target Locking Hypothesis

- Implication for non-optimal strategies, after the Half-Half rule $\rightarrow$
Attentional gating should aim to allocate more capacity resources to the target than to memorized items.



## The model

## The Exemplar-Based STM Retrieval Model EBRW and the ItemTarget Product Rule

Capacity
Distributed via Attentional Gating


Time
e.g. Nosofsky, Little ,Donkin, \& Fific, 2011

## New Method

## The attention-to-position paradigm

- Rapid short-term memory paradigm
- Focal set : To pay special attention to certain item positions in the memorized list, called a "focal set". This means that if a target item was a member of a focal set, a response decision had to be extremely fast, and accurate
- Peripheral set: The rest items not contained in a focal set.



## New Method

## The attention-to-position paradigm

- To prevent interference of extraneous variables with the process of resource allocation the subjects were instructed to pronounce each item in a set, without accentuation, and with a monotonic prosody
- Two measures: mean response time (RT) and accuracy.


## The data





- This is a typical RT pattern observed in the STM research, the primacy and recency
(1) Equal-precision
(2) ALLOR NONE
(3) The decay-representation WM model
(4) Fluid-resource model
(5) Slots+averaging model


## The data



- This is a typical pattern observed in the STM research, the primacy and recency
(1) Equal-precision
(2) ALL-OR-NONE
(3) Decay representation WM model
(4) Fluid-resource model
(5) Slots+averaging model


## Comparison



- Implications
- A discontinuous serial position effect -> Dual WM systems
- The principle of resource conservation-> Strictly fixed capacity


## The data - further validation of resource allocation





## Comparison



## The proposed resource allocation model :The Tilted Water Tank



Equal




## Model fitting: the linear distribution function of resource allocation

## Estimated Capacity Allocations


discrete-slot model
slots+averaging model

variable-resources model


## How many boxes?

- Conduct data fitting of the EBRW model that can freely allocate fixed amount of resources across memorized items, including the parameter which defines a number of possible memory slots (boxes).
- In other words: find the number of possible resource allocation units (slots, boxes) that maximizes the goodness of fit of the model for resource allocation.


## How many boxes?

Free resource parameter-EBRW mode

| Params | All Fast | First Three | Last <br> Three |
| :---: | :---: | :---: | :---: |
| C | 0.959 | 2.383 | 1.6 |
| acrit | 2.52 | 3.556 | 11.378 |
| bcrit | 3.936 | 43.592 | 17.164 |
| scale | 44.706 | 4.576 | 1.901 |
| mu | 175.816 | 137.859 | 256.035 |
| listbase | 0.175 | 0.261 | 0.42 |
| dscale | 2.705 | 0.979 | 0.65 |
| m1 | 0.14 | 0.161 | 0.128 |
| m2 | 0.131 | 0.166 | 0.131 |
| m3 | 0.132 | 0.167 | 0.128 |
| m4 | 0.161 | 0.170 | 0.176 |
| m5 | 0.201 | 0.172 | 0.208 |
| m6 | 0.231 | 0.164 | 0.229 |
| boxes | 801 | 670 | 711 |

## Conclusions

$\square$ New method for testing WM, attention by instruction
$\square$ Support for the variable-resources model WM, all-get-some
$\square$ Falsification of all-or-none approaches, discrete representations
$\square$ We specified a likely mechanism of resource allocation (Target locking) and provided rationale
$\square$ The ghost is likely to reside in a tilted tank!

Further Implications:
$\square$ Linear distribution function of resources could serve as a proxy to the Attentional Gating mechanism.
$\square$ Falsification of Dual system WM view: the last item position advantage
$\square$ A joint fit of mean RT and choice probabilities.[EBRW]
$\square$ A STM capacity resources are strictly limited (the conservation of resources principle)

## Free allocation of fixed capacity model

2D Graph 1


